

Name:

Registration Number:

NATIONAL EXAMINATIONS COUNCIL
Senior School Certificate Examination


1 hour 45 minutes

GENERAL MATHEMATICS
PAPER III

Do not open this question booklet until you are told to do so. While waiting, read the following carefully:

1. Use **HB** pencil throughout.
2. Use of **mobile phone is not allowed**.
3. Use of **scientific calculator is allowed**.
4. **All diagrams are not drawn to scale.**
5. Take π to be $\frac{22}{7}$ **except** otherwise stated.
6. Where your answer sheet is **not** customised, provide the following information:
 - (a) In the space marked *Candidate's Name*, write your surname in capital letters followed by your **other** names.
 - (b) In the space marked *School Name*, write the name of your school, and in the space marked *Subject Name*, write **General Mathematics III**.
 - (c) In the box marked *Subject Code*, write the digits **1023** in the spaces. There are numbered spaces in line with each digit. Shade carefully the space with the same number as each digit.
 - (d) In the box marked *Registration Number*, write your **registration number** in the spaces at the top of the box. Shade the corresponding numbered spaces in the same way as for Subject Code.
7. An example is given below. This is for a candidate whose name is **GAMBO Bamidele Uche**, with serial number 0010, registration number 8765432100BD, and who is taking **General Mathematics III (1023)**.

National Examinations Council ANSWER SHEET

Use HB pencil to complete this form. Mark like this . Erase errors thoroughly.

Examination Type SSCE <input checked="" type="checkbox"/> BECE <input type="checkbox"/> (i) (ii) <input type="checkbox"/> <input type="checkbox"/> Other <input type="checkbox"/> If Other, write exam type in the box below Absent <input type="checkbox"/>	Candidate's Serial No. in School 0 0 1 0 (1) (1) (0) (1) (2) (2) (2) (2) (3) (3) (3) (3) (4) (4) (4) (4) (5) (5) (5) (5) (6) (6) (6) (6) (7) (7) (7) (7) (8) (8) (8) (8) (9) (9) (9) (9)	Subject Code 1 0 2 3 (0) (0) (0) (0) (1) (1) (1) (1) (2) (2) (2) (2) (3) (3) (3) (3) (4) (4) (4) (4) (5) (5) (5) (5) (6) (6) (6) (6) (7) (7) (7) (7) (8) (8) (8) (8) (9) (9) (9) (9)	Registration Number 8 7 6 5 4 3 2 1 0 0 B D (0) (0) (0) (0) (0) (0) (0) (0) (0) (0) (0) (0) (1) (1) (1) (1) (1) (1) (1) (1) (1) (1) (1) (1) (2) (2) (2) (2) (2) (2) (2) (2) (2) (2) (2) (2) (3) (3) (3) (3) (3) (3) (3) (3) (3) (3) (3) (3) (4) (4) (4) (4) (4) (4) (4) (4) (4) (4) (4) (4) (5) (5) (5) (5) (5) (5) (5) (5) (5) (5) (5) (5) (6) (6) (6) (6) (6) (6) (6) (6) (6) (6) (6) (6) (7) (7) (7) (7) (7) (7) (7) (7) (7) (7) (7) (7) (8) (8) (8) (8) (8) (8) (8) (8) (8) (8) (8) (8) (9) (9) (9) (9) (9) (9) (9) (9) (9) (9) (9) (9)											
			Candidate's Name		GAMBO Bamidele Uche									
			School Number		0210231									
			School Name		Government Secondary School, Minna									
			Subject Name		General Mathematics III									

PAPER III
Answer all questions.

Each question is followed by five options lettered A to E. Choose the correct option for each question and shade in pencil on your answer sheet the answer space that bears the same letter as the option you have chosen. Give only one answer to each question and erase completely any answer you wish to change. Do all rough work on this question paper.

An example is given below:

The product of three numbers is 3876. Two of the numbers are 17 and 19. What is the third number?

- A. 57
- B. 12
- C. 6
- D. 3
- E. 2

The correct option is '12' which is lettered B. Therefore, answer space B would be shaded as shown below:

	[A]	<input checked="" type="radio"/> [B]	[C]
1.	Express 384.126 to the nearest hundred.		
	A. 480		
	<input checked="" type="radio"/> B. 400		
	C. 384		
	D. 380		
	E. 300		
$384.126 = \underline{400}$			
2.	If $A = \{\text{natural numbers between 3 and 15}\}$, find $n(A)$.		
	A. 15		
	B. 14		
	C. 13		
	<input checked="" type="radio"/> D. 11		
	E. 10		
$n(A) = 4, 5, 6, 7, 8, 9, 10, 11, 12, 13 \text{ and } 14.$			
$\Rightarrow n(A) = \underline{11}$			
3.	Evaluate $3241_{\text{five}} - 1342_{\text{five}}$.		
	A. 2341_{five}		
	<input checked="" type="radio"/> B. 1344_{five}		
	C. 1342_{five}		
	D. 1324_{five}		
	E. 1234_{five}		
$\begin{array}{r} 3241 \\ -1342 \\ \hline 1344 \end{array}$			
$\Rightarrow 3241_{\text{five}} - 1342_{\text{five}} = 1344_{\text{five}}$			

	[D]	[E]
4.	Simplify $(4\sqrt{3}-6)(4\sqrt{3}+6)$.	
	<input checked="" type="radio"/> A. 12	
	B. 4	
	C. $2\sqrt{3}$	
	D. 2	
	E. $\sqrt{3}$	
$\begin{aligned} &\text{Conjugate binomial surd} \\ &\Rightarrow (4\sqrt{3}-6)(4\sqrt{3}+6) \\ &= 16 \times 3 - 36 \\ &= 48 - 36 \\ &= \underline{12} \end{aligned}$		
5.	The third term of a Geometric Progression is -5 and the seventh term is -80. Find the common ratio.	
	A. 16	
	B. 8	
	C. 5	
	D. 3	
	<input checked="" type="radio"/> E. 2	
$\begin{aligned} &q r^{n-1} \\ &\Rightarrow 3^{\text{rd}} \text{ term} = q r^{3-1} = -5 \\ &= q r^2 = -5 \\ &q = \frac{-5}{r^2} \end{aligned}$		
$\Rightarrow q = \frac{-5}{r^2} \dots (i)$		
$\begin{aligned} &7^{\text{th}} \text{ term} = q r^{7-1} = -80 \\ &q r^6 = -80 \end{aligned}$		
$\Rightarrow q = \frac{-80}{r^6} \dots (ii)$		
$\text{Comparing both equations}$		
$\frac{-5}{r^2} = \frac{-80}{r^6}; \frac{r^6}{r^2} = \frac{-80}{-5}$		
$\Rightarrow r^4 = 16; \Rightarrow r = \sqrt[4]{16} = \underline{2}$		

6. A man with an annual salary of ₦1,300,000.00 is to pay an income tax of 22%. Calculate his tax, if his allowances amount to ₦137,000.00.

- A. ₦254,760.00
 B. ₦255,860.00
 C. ₦258,860.00
 D. ₦350,140.00
 E. ₦907,140.00
- Income tax is Salary - Allowance*
 $\text{₦}1,300,000 - \text{₦}137,000 = \text{₦}1,163,000$
 $\Rightarrow \text{tax} = 22\% \times \frac{\text{₦}1,163,000}{100\%}$

7. A wire of length 25 cm was measured by a student to be 24.4 cm. Find the percentage error.

- A. 4.4
 B. 3.4
 C. 2.4
 D. 1.4
 E. 0.4
- $\% \text{ error} = \frac{\text{error} \times 100\%}{\text{actual length}}$
 $\text{error} = 25 - 24.4 = 0.6$
 $\Rightarrow \% \text{ error} = \frac{0.6 \times 100\%}{25} = 2.4$

8. How many years will ₦12,000.00 saved in a bank amount to ₦12,960.00 at 2% per annum simple interest?

- A. 6
 B. 5
 C. 4
 D. 3
 E. 2
- $\text{Amount} = I + P$
 $\Rightarrow \text{₦}12,960 = I + \text{₦}12,000$
 $\Rightarrow I = \text{₦}960$
 $I = \frac{PRT}{100\%}; 960 = \frac{12,000 \times T}{2 \times 100\%}$
 $\Rightarrow T = \frac{96,000}{24,000} = 4 \text{ years}$

9. Rationalize $\frac{5}{\sqrt{2} + \sqrt{3}}$.

- A. $5(\sqrt{3} - \sqrt{2})$
 B. $5(\sqrt{2} + \sqrt{3})$
 C. $5(\sqrt{2} - \sqrt{3})$
 D. $\sqrt{3} + 5\sqrt{2}$
 E. $\sqrt{3} + 2\sqrt{5}$

$\frac{5}{\sqrt{2} + \sqrt{3}}$ Rationalizing denominator

$\frac{5}{\sqrt{2} + \sqrt{3}} \times \frac{\sqrt{2} - \sqrt{3}}{\sqrt{2} - \sqrt{3}}$

$\Rightarrow \frac{5(\sqrt{2} - \sqrt{3})}{2 - 3}$

$\Rightarrow \frac{5(\sqrt{2} - \sqrt{3})}{-1}$

$\Rightarrow -5(\sqrt{2} - \sqrt{3})$ multiply by +

$\Rightarrow 5(\sqrt{2} + \sqrt{3})$

10. In a class of 80 students, every student studies Mathematics or Geography or both. If 65 students study Mathematics and 50 study Geography, how many study both subjects?

- A. 45
 B. 35
 C. 30
 D. 20
 E. 15
- M* *G*
- $65 - x$ x $50 - x$
- $\Rightarrow 65 - x + x + 50 - x = 80$
 $115 - x = 80$
 $\Rightarrow x = 115 - 80; x = 35$

11. The 11th term of an Arithmetic Progression is 63. Find the first term, if its common difference is 3.

- A. 65
 B. 63
 C. 35
 D. 33
 E. 30
- $T_n = a + (n-1)d$
 $63 = a + (11-1)3$
 $63 = a + 30$
 $\Rightarrow a = 63 - 30 = 33$

12. Evaluate $15 \otimes 26$ in modulo 5.

- A. 0 (mod 5)
 B. 1 (mod 5)
 C. 2 (mod 5)
 D. 4 (mod 5)
 E. 5 (mod 5)
- $15 \otimes 26 \pmod{5}$
 $15 \otimes 26 = 390$
 $\Rightarrow \frac{390}{5} = 78 \text{ Rem. } 0$
 $\Rightarrow 15 \otimes 26 = 0 \pmod{5}$

13. Solve $2^{3x} = 16^{\frac{3}{4}}$.

- A. 8
 B. 4
 C. 3
 D. 2
 E. 1
- $2^{3x} = 16^{\frac{3}{4}}$
 Raising both sides to same base
 $\Rightarrow 2^{3x} = (2^4)^{\frac{3}{4}}$
 $2^{3x} = 2^{12/4}$
 $\Rightarrow 2^{3x} = 2^3$
 Striking off the similar base on both sides
 $\Rightarrow 2^{3x} = 2^3$
 $\Rightarrow 3x = 3$
 $\Rightarrow x = \frac{3}{3} = 1$

14. If Olu, Tony and Tunde share ₦240,000.00 in the ratio 2:3:5 respectively, what is two-thirds of Tunde's share?

- A. ₦120,000.00
- B. ₦80,000.00
- C. ₦72,000.00
- D. ₦48,000.00
- E. ₦40,000.00

Total ratio = 10
 Tunde = $\frac{5}{10} (\text{₦}240,000)$
 $= \frac{1,200,000}{10}$
 $= \text{₦}120,000$
 $\Rightarrow \frac{2}{3} (\text{₦}120,000)$
 $= \text{₦}80,000$

15. Arrange the following fractions in ascending order of magnitude;
 $\frac{2}{3}, \frac{3}{5}, \frac{5}{12}, \frac{4}{15}, \frac{3}{10}$

- (A) $\frac{4}{15}, \frac{3}{10}, \frac{5}{12}, \frac{3}{5}, \frac{2}{3}$
- B. $\frac{3}{10}, \frac{4}{15}, \frac{5}{12}, \frac{3}{5}, \frac{2}{3}$
- C. $\frac{4}{15}, \frac{5}{12}, \frac{3}{10}, \frac{3}{5}, \frac{2}{3}$
- D. $\frac{4}{15}, \frac{5}{12}, \frac{3}{5}, \frac{3}{10}, \frac{2}{3}$
- E. $\frac{2}{3}, \frac{3}{5}, \frac{5}{12}, \frac{4}{15}, \frac{3}{10}$

16. Find the values of x, y and z respectively for which

$$\begin{bmatrix} x & 2y \\ z & 9 \end{bmatrix} = \begin{bmatrix} 4 & 12 \\ 3 & 9 \end{bmatrix}$$

- A. (6, 4, 3)
- (B) (4, 6, 3)
- C. (6, 3, 4)
- D. (3, 4, 6)
- E. (4, 4, 6)

$$\begin{bmatrix} x & 2y \\ z & 9 \end{bmatrix} = \begin{bmatrix} 4 & 12 \\ 3 & 9 \end{bmatrix}$$

$\Rightarrow x = 4$
 $2y = 12; y = \frac{12}{2} = 6$
 $z = 3$
 $\Rightarrow x, y \text{ and } z = 4, 6, 3$

17. If $P = \begin{bmatrix} -1 & 2 \\ 3 & 1 \end{bmatrix}$ and $Q = \begin{bmatrix} 2 & 3 \\ 2 & 1 \end{bmatrix}$, find PQ.

- A. $\begin{bmatrix} 2 & 1 \\ -8 & -10 \end{bmatrix}$
- B. $\begin{bmatrix} 2 & 1 \\ 8 & 10 \end{bmatrix}$
- C. $\begin{bmatrix} -2 & 1 \\ 8 & 10 \end{bmatrix}$
- D. $\begin{bmatrix} -2 & -1 \\ 8 & 10 \end{bmatrix}$
- (E) $\begin{bmatrix} 2 & -1 \\ 8 & 10 \end{bmatrix}$

$$PQ = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix} = \begin{bmatrix} 2 & -1 \\ 8 & 10 \end{bmatrix}$$

$a_{11} = (-1 \ 2) \begin{pmatrix} 2 \\ 2 \end{pmatrix}$
 $= -1 \times 2 + 2 \times 2 = 2$
 $a_{12} = (-1 \ 2) \begin{pmatrix} 3 \\ 1 \end{pmatrix}$
 $= -1 \times 3 + 2 \times 1 = -1$
 $a_{21} = (3 \ 1) \begin{pmatrix} 2 \\ 2 \end{pmatrix}$
 $= 6 + 2 = 8$
 $a_{22} = (3 \ 1) \begin{pmatrix} 3 \\ 1 \end{pmatrix}$
 $= 9 + 1 = 10$

18. Evaluate $\log_4 16 + \log_3 27 - \log_8 4096$.

- A. $\frac{1}{9}$
- B. $\frac{1}{3}$
- (C) 1
- D. 2
- E. 3

$$\log_4 16 + \log_3 27 - \log_8 4096$$

$\Rightarrow 2 \log_4 4 + 3 \log_3 3 - 4 \log_8 8$
 $\Rightarrow 2(1) + 3(1) - 4(1)$
 $\Rightarrow 2 + 3 - 4 = 1$

19. Solve the equation $\frac{4x}{5} - \frac{7}{3} = \frac{5x}{12}$.

- A. $-6\frac{2}{23}$
- B. $-3\frac{1}{2}$
- C. $5\frac{2}{23}$
- (D) $6\frac{2}{23}$
- E. $6\frac{3}{23}$

$$\frac{4x}{5} - \frac{7}{3} = \frac{5x}{12}$$

$(12 \times 4x) - (20 \times 7) = (5 \times 5x)$
 $48x - 140 = 25x$
 $48x - 25x = 140$
 $23x = 140$
 $x = \frac{140}{23}$
 $= 6\frac{2}{23}$

20. If $f(x) = 3x^2 - 9x - 5$, find $f(-3)$.

- A. -5
 B. 5
 C. 27
 D. 49
 E. 54
- $$f(-3) = 3(-3)^2 - 9(-3) - 5$$
- $$= 3(9) + 27 - 5$$
- $$= 27 + 22$$
- $$= \underline{\underline{49}}$$

21. Find u in terms of f and v in the relation $\frac{1}{v} = \frac{1}{f} - \frac{1}{u}$.

- A. $u = \frac{-f}{(v-f)}$
 B. $u = \frac{fv}{(f-v)}$
 C. $u = \frac{fv}{(v+f)}$
 D. $u = \frac{fv}{(v-f)}$
 E. $u = \frac{fv}{2(f+v)}$
- $\frac{1}{v} = \frac{1}{f} - \frac{1}{u}$
 Inverting both sides of the equations;
 $v = f - u$
 $\Rightarrow u = f - v$
 Same as $u = \frac{fv}{(v-f)}$
 i.e. $f - v = \frac{fv}{(v-f)}$
 $= \frac{fv}{v-f} = \frac{fv}{-(f-v)} = -\frac{fv}{f-v}$

22. Find the quadratic equation whose roots are -1 and 5 .

- A. $x^2 - 4x - 5 = 0$
 B. $x^2 - 4x + 1 = 0$
 C. $x^2 - 4x + 5 = 0$
 D. $x^2 + 4x - 5 = 0$
 E. $x^2 + 4x + 5 = 0$
- Using the formula
 $x^2 - (\alpha + \beta)x + \alpha\beta$
 $x^2 - (-1 + 5)x + (-1 \times 5)$
 $x^2 - (4)x + (-5)$
 $x^2 - 4x - 5 = 0$

23. The product of two numbers is 40 and their sum is 13, find the numbers.

- A. 2 and 20
 B. 2 and 8
 C. 4 and 10
 D. 4 and 8
 E. 5 and 8
- Let the two numbers be x and y . Then,
 $xy = 40$; $x + y = 13$
 from $x + y = 13$
 $y = 13 - x$
 Substituting for y in the first equation
 $xy = 40$; $x(13 - x) = 40$
 $\Rightarrow 13x - x^2 = 40$
 $\Rightarrow x^2 - 13x + 40 = 0$
 $\Rightarrow (x - 8)(x - 5) = 0$
 $\Rightarrow x = 8$ or 5
 $\Rightarrow x$ and $y = 5$ and 8

24. If $(x+6)$ is a factor of $x^2 + 4x - 12$, find the other factor.

- A. $(x-2)$
 B. $(x-6)$
 C. $(x+2)$
 D. $(x+4)$
 E. $(x+6)$

Factors will multiply the equation to give zero.
 Therefore, we test from the options
 $(x-2)$; $x=2$; $(2)^2 + 4(2) - 12$
 $4 + 8 - 12 = 0 \checkmark$
 $(x-6)$; $x=6$; $(6)^2 + 4(6) - 12$
 $36 + 24 - 12 = 48 \neq 0$

25. Calculate the mid-point of the line joining $(8, -3)$ and $(-2, 3)$.

- A. $(-3, 0)$
 B. $(0, 5)$
 C. $(3, 0)$
 D. $(0, 3)$
 E. $(5, 0)$

The mid points on the x and y axes are;
 $\frac{x_1 + x_2}{2}$ and $\frac{y_1 + y_2}{2}$
 $\frac{8 + (-2)}{2} = 3$; $\frac{-3 + 3}{2} = 0$
 $(3, 0)$

26. Calculate the gradient of a line joining the points $(-2, -5)$ and $(4, 8)$, correct to 1 decimal place.

- A. 4.2
 B. 3.4
 C. 3.2
 D. 2.2
 E. 2.1

Gradient $M = \frac{y_2 - y_1}{x_2 - x_1}$
 $\Rightarrow M = \frac{8 - (-5)}{4 - (-2)} = \frac{13}{6}$
 $= \underline{\underline{2.2}}$

27. Given the statements:

- p : All terrorists are guilty
 q : All terrorists are criminals
 Write the following statement in symbolic form; "All terrorists are not guilty but criminals".

- A. $p \vee q$
 B. $p \wedge q$
 C. $p \wedge \sim q$
 D. $\sim p \vee q$
 E. $\sim p \wedge q$

$\sim p \vee q$ is either ways
 while
 $\sim p \wedge q$ is Conclusive or specific as the question.

$\sim p \wedge q =$ All terrorists are not guilty, and all terrorists are criminals.

From the question: "All terrorists are not guilty but criminals"

And (\wedge) can be used to represent the but as both are specific in the context of the qst. While (\vee) is either ways

28. Simplify $\frac{x + \frac{1}{3}}{x + \frac{1}{2}}$

(A) $\frac{2(3x+1)}{3(2x+1)}$ $\left(\frac{x + \frac{1}{3}}{\frac{3x+1}{3}}\right) \div \left(\frac{x + \frac{1}{2}}{\frac{2x+1}{2}}\right)$

B. $\frac{2+x}{3+x}$ $\frac{3x+1}{3} \times \frac{2}{2x+1}$

C. $\frac{x+1}{x-1}$ $\Rightarrow \frac{2(3x+1)}{3(2x+1)}$

D. $\frac{3x+1}{2x-1}$

E. $\frac{x^2}{x-1}$

29. Find the equation of a line whose gradient is 6 and y-intercept is -7.

A. $y = 8 + 7x$

B. $y = -7 - 6x$

C. $y = 7 - 6x$

(D) $y = -7 + 6x$

E. $y = 7 + 6x$

Using the form $y = mx + c$
 $y = 6x + (-7)$
 $y = 6x - 7$
 $y = -7 + 6x$

30. Find the sum of the roots of the quadratic equation $x^2 - 5x + 6 = 0$.

A. 10

(B) 5

C. -2

D. -3

E. -5

$x^2 - 5x + 6 = 0$
 $x^2 - 3x - 2x + 6 = 0$
 $\Rightarrow x = 3$ or 2
 $\Rightarrow 3 + 2 = 5$

31. Find the roots of the equation $8x^2 - 6x - 9 = 0$.

A. $x = \frac{3}{2}$ or $-\frac{4}{3}$

B. $x = \frac{3}{2}$ or $-\frac{3}{4}$

C. $x = \frac{3}{2}$ or $\frac{3}{4}$

(D) $x = -\frac{3}{2}$ or $\frac{3}{4}$

E. $x = -\frac{3}{2}$ or $-\frac{3}{4}$

$8x^2 - 6x - 9 = 0$
 $8x^2 + 12x - 6x - 9 = 0$
 $4(2x+3) - 3(2x+3) = 0$
 $(4x-3)(2x+3) = 0$
 $\Rightarrow 4x = 3, 2x = -3$
 $\Rightarrow x = \frac{3}{4}$ or $-\frac{3}{2}$

32. Expand $(2x - 3)(3x + 4)$.

A. $6x^2 - 17x - 12$

(B) $6x^2 - x - 12$

C. $6x^2 - x + 12$

D. $6x^2 + x - 12$

E. $6x^2 + 17x - 12$

$6x^2 + 8x - 9x - 12$
 $6x^2 - x - 12$

33. The difference between the present ages of two brothers is 6 and their product is 135. What is the sum of their ages?

A. 27

(B) 24

C. 22

D. 21

E. 15

Let the younger age be x , then the old age is $x + 6$
 \Rightarrow their product is $x(x + 6) = 135$
 $\Rightarrow x^2 + 6x = 135; x^2 + 6x - 135 = 0$
 $\Rightarrow x^2 + 15x - 9x - 135 = 0$
 $x(x + 15) - 9(x + 15) = 0$
 $\Rightarrow (x - 9)(x + 15) = 0$
 $\Rightarrow x - 9 = 0$ or $x + 15 = 0$
 $\Rightarrow x = 9$ or $x = -15$
 $\Rightarrow x = 9$ and the older age is $9 + 6 = 15$
 \Rightarrow the ages are 9 and 15
 and their sum = $9 + 15 = 24$

34. In Fig. 3.1, PQS is a circle with centre O. RST is a tangent at S and $\angle SOP = 120^\circ$. Find $\angle PST$.

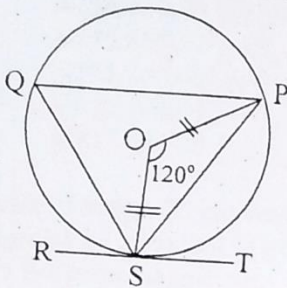


Fig. 3.1 $\triangle SOP$ is isosceles

- A. 64°
 (B) 60°
 C. 35°
 D. 31°
 E. 29°
- $\Rightarrow \angle OSP = \frac{1}{2}(180 - 120) = 30^\circ$
 $\angle OST = 90^\circ$ (\perp tan. radius)
 $\Rightarrow \angle PST = 90 - 30 = 60^\circ$

35. In Fig. 3.2, A, B, C and D are points on a circle with centre O. \overline{BA} is produced to M. If $\angle MAD = 82^\circ$ and $\angle ADO = 74^\circ$, find $\angle ABO$.

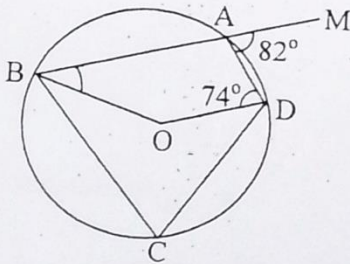


Fig. 3.2

- (A) 24°
 B. 74°
 C. 82°
 D. 98°
 E. 164°

$\angle BCD = 82^\circ$ (exterior \angle of cyclic quad. is equal to interior opp. \angle)

$\angle BOD = 2 \times 82^\circ$ (\angle at center is twice \angle at circumference)
 $= 164^\circ$

$\angle DAB = 180 - 82^\circ$ (\angle on straight line)
 $= 98^\circ$

$\Rightarrow \angle ABO = 360 - (74 + 164 + 98)$
 (sum of interior quad.)
 $= 360 - 336 = 24^\circ$

36. Calculate the area of trapezium ABCD in Fig. 3.3.

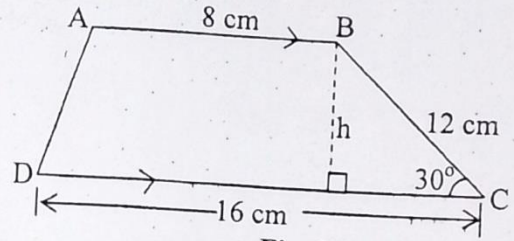


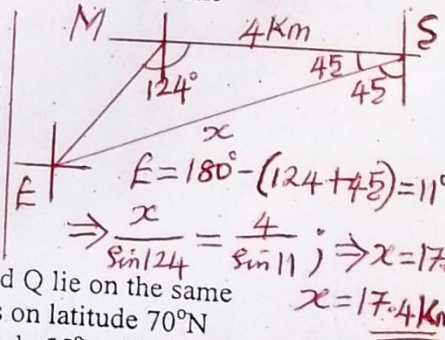
Fig. 3.3

- A. 27 cm^2
 B. 36 cm^2
 (C) 72 cm^2
 D. 92 cm^2
 E. 144 cm^2

Area of trapezium $\frac{1}{2}h(l_1 + l_2)$
 $h = 12 \times \sin 30^\circ = 12 \times 0.5 = 6$
 \Rightarrow Area of Trap $= \frac{1}{2} \times 6(8 + 16) = 3(24) = 72 \text{ cm}^2$

37. A boy walks 4 km due West. He then changes direction and walks on a bearing of 214° until he is South-West of his starting point. How far is he from his starting point? Correct your answer to one decimal place.

- A. 5.1 km
 B. 8.3 km
 C. 11.1 km
 D. 15.7 km
 (E) 17.4 km



38. Two points P and Q lie on the same great circle. P is on latitude 70°N and Q is on latitude 55°N . Calculate their difference in latitudes:

- (A) 15°
 B. 25°
 C. 45°
 D. 65°
 E. 125°

Their difference in latitude is $70 - 55 = 15^\circ$

39. A bird which is on top of a building 35 m high observes a prey 25 m away from the foot of the building. Calculate the angle of depression of the prey from the bird.

A. 75.00°
 B. 60.00°
 C. 54.46°
 D. 35.25°
 E. 10.00°

Angle of Dep. = α
 $\tan \alpha = \frac{35}{25} = 1.4$
 $\Rightarrow \alpha = \tan^{-1} 1.4 = 54.5^\circ$

40. Calculate the length of an arc which subtends an angle of 66° at the centre of a circle of radius 8 cm, correct to one decimal place.

A. 3.4 cm
 B. 5.2 cm
 C. 7.4 cm
 D. 9.2 cm
 E. 12.3 cm

Length of arc = $\frac{\theta}{360} \times 2\pi r$
 $\frac{66}{360} \times 2 \times 3.143 \times 8$
 $\frac{3319.008}{360} = 9.2 \text{ cm}$

41. Find the value of y in Fig. 3.4.

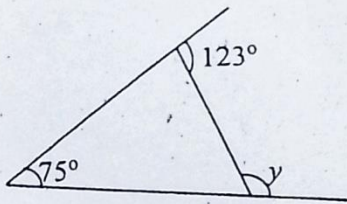
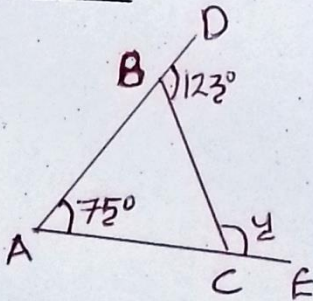


Fig. 3.4

- A. 48°
 B. 57°
 C. 105°
 D. 132°
 E. 198°



$\angle ABC = 180 - 123$ (straight line)
 $= 57^\circ$
 $\Rightarrow y = 75 + 57$ (ext. \angle of triangle)
 $= 132^\circ$

42. The base radius and height of a cone are 4 cm and 6 cm respectively. Calculate its volume, correct to the nearest whole number.

A. 75 cm³
 B. 86 cm³
 C. 98 cm³
 D. 101 cm³
 E. 110 cm³

Volume of cone = $\frac{1}{3} \pi r^2 h$
 $= \frac{1}{3} \times 3.143 \times 4^2 \times 6$
 $= \frac{301.728}{3} = 100.6$
 $\approx 101 \text{ cm}^3$

43. Find the distance between the points (3, -4) and (-5, 2).

A. 18
 B. 16
 C. 14
 D. 12
 E. 10

$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$
 $\sqrt{(-5 - 3)^2 + (2 - (-4))^2}$
 $\sqrt{(-8)^2 + 6^2}; \sqrt{64 + 36} = 10$

44. Calculate the surface area of a sphere with diameter 10.4 cm, correct to 3 significant figures. (Take $\pi = 3.142$)

A. 439 cm²
 B. 400 cm²
 C. 340 cm²
 D. 339 cm²
 E. 338 cm²

Surface area of sphere = $4\pi r^2$
 $r = \frac{1}{2} \text{ diameter} = \frac{1}{2} \times 10.4 = 5.2$
 $\Rightarrow \text{S. Area} = 4 \times 3.142 \times 5.2^2 = 340 \text{ cm}^2$

45. Obi walks 400 m to the top of a hill which slopes at angle 30° to the horizontal. Determine the height of the hill.

A. 430 m
 B. $400\sqrt{3}$ m
 C. $200\sqrt{3}$ m
 D. 200 m
 E. 100 m

$h = 400 \sin 30^\circ$
 $= 400 \times 0.5$
 $= 200 \text{ m}$

53. Calculate the variance of the following set of numbers; $\bar{x} = \frac{155}{5} = 31$
30, 28, 35, 25, 37.

	x	x - \bar{x}	d ²	
A.	31.0			$\text{Var } \sigma^2 = \frac{\sum d ^2}{n}$ $\sum d ^2 = 98$ $n = 5$ $\Rightarrow \sigma^2 = \frac{98}{5} = 19.6$
B.	25.1	-6	36	
C.	19.6	-3	9	
D.	19.5	-1	1	
E.	15.3	4	16	

54. If the tickets numbered 1 to 16 inclusive are mixed up and a ticket is drawn at random, what is the probability that the ticket drawn is a multiple of 2 or 3?

- A. $\frac{5}{16}$ | 1 to 16 inclusive = 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15 and 16
- B. $\frac{1}{2}$ | 15 and 16
- C. $\frac{5}{8}$ | Multiples of 2 = 2, 4, 6, 8, ... 16
Multiples of 3 = 3, 6, 9, ... 15
- D. $\frac{11}{16}$ | \Rightarrow Multiples of 2 are 8
Multiples of 3 are 5
- E. $\frac{13}{16}$ | $\Rightarrow P(\text{mult. of 2 or 3}) = \frac{8}{16} + \frac{5}{16} = \frac{13}{16}$

55. The following are the lucky numbers in a raffle draw; 4, 5, 12, 20, 2, 8, 3, 6, 10, 9, 7, 25, 12, 10, 14, 27.

If a number is picked at random, what is the probability that it is a perfect cube?

- A. $\frac{11}{16}$ | The perfect cube from the set of numbers are 8 and 27 only
- B. $\frac{5}{8}$ | 8 and 27 only
- C. $\frac{7}{16}$ | $\Rightarrow P(\text{perfect cube}) = \frac{2}{16}$
- D. $\frac{3}{8}$ | $= \frac{1}{8}$
- E. $\frac{1}{8}$ | $= \frac{1}{8}$

56. The probability that it will rain in Lagos and Oyo on the same day are $\frac{3}{4}$ and $\frac{1}{2}$ respectively. Find the probability that it will not rain in both towns on the same day.

- A. $\frac{1}{12}$
- B. $\frac{1}{8}$
- C. $\frac{1}{6}$
- D. $\frac{1}{4}$
- E. $\frac{1}{2}$

$P(\text{it will rain in both}) = \frac{3}{4} \times \frac{1}{2} = \frac{3}{8}$
 $P(\text{it will not rain in both cities}) = \frac{1}{4} \times \frac{1}{2} = \frac{1}{8}$

57. Table 3.1: Ages of students

Age (years)	16	17	18
No of students	4	8	6

Table 3.1 shows the ages of students in a particular class. What is the probability that a student chosen at random is less than 18 years?

- A. $\frac{9}{10}$
- B. $\frac{4}{5}$
- C. $\frac{2}{3}$
- D. $\frac{1}{2}$
- E. $\frac{1}{3}$

Sample space $S = 4 + 8 + 6 = 18$
 $P(\text{less than 18}) = \frac{4}{18} + \frac{8}{18}$
 $= \frac{12}{18}$
 $= \frac{2}{3}$

Use the information below to answer questions 58 - 60.

A particle moves a distance of S metres, where $S = 5t^3 - 12t^2 + 7$.

58. At what time is its acceleration equals zero?

- A. 0.8 sec
- B. 1.2 sec
- C. 1.6 sec
- D. 2.0 sec
- E. 2.5 sec

59. Find the velocity after 3 seconds.

- A. 70 m/s
- B. 63 m/s
- C. 50 m/s
- D. 40 m/s
- E. 30 m/s

60. Find the acceleration after 12 seconds.

- A. 400 m/s²
- B. 360 m/s²
- C. 336 m/s²
- D. 300 m/s²
- E. 180 m/s²